

**INTERNATIONAL STUDIES in SCIENCE and ENGINEERING**

**Roman Weber**

**LECTURE NOTES**

**IN**

**HEAT TRANSFER**

**3<sup>rd</sup> Edition**



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